

Properties for Expressions:	
$x = 1x$	$-x = -1x$
$nx = \underbrace{x + \dots + x}_{n\text{-many times}}$	
$x - x = 0$	
$a - b = a + -b$	
Multiple instances of addition can be performed in any order. For example: $a + b = b + a$ $(a + b) + c = a + b + c$ $a + (b + c) = a + b + c$	
Multiple instances of multiplication can be performed in any order. For example: $ab = ba$ $(ab)c = abc$ $a(bc) = abc$	
$a(b + c) = ab + ac$	$(a + b)c = ac + bc$
$a(x_1 + \dots + x_n) = ax_1 + \dots + ax_n$	$(x_1 + \dots + x_n)c = x_1c + \dots + x_nc$
$x^n = \underbrace{x \cdot \dots \cdot x}_{n\text{-many times}}$	
$x^{-n} = \frac{1}{x^n}$ (whenever $x \neq 0$)	
$\frac{x}{1} = x$	
$\frac{x}{x} = 1$ (whenever $x \neq 0$)	
$\frac{ab}{cd} = \frac{a}{c} \cdot \frac{b}{d}$ (whenever $c, d \neq 0$)	$\frac{x_1 \cdot \dots \cdot x_n}{y_1 \cdot \dots \cdot y_n} = \frac{x_1}{y_1} \cdot \dots \cdot \frac{x_n}{y_n}$ (whenever $y_1, \dots, y_n \neq 0$)
$\frac{a+b}{c} = \frac{a}{c} + \frac{b}{c}$ (whenever $c \neq 0$)	$\frac{x_1 + \dots + x_n}{y} = \frac{x_1}{y} + \dots + \frac{x_n}{y}$ (whenever $y \neq 0$)
$\sqrt[n]{x^n} = \begin{cases} x & \text{if } n \text{ is odd or } x \geq 0 \\ -x & \text{if } n \text{ is even and } x < 0 \end{cases}$	
$\sqrt[n]{ab} = \sqrt[n]{a} \sqrt[n]{b}$	for example, $\sqrt{x} \cdot \sqrt{x} = \sqrt{x \cdot x} = \sqrt{x^2}$
$\sqrt[n]{\frac{a}{b}} = \frac{\sqrt[n]{a}}{\sqrt[n]{b}}$ (whenever $b \neq 0$)	
$ax^2 + bx + c = ax^2 + b_1x + b_2x + c$ * b_1, b_2 are whole numbers whenever * $b_1 \cdot b_2 = ac$ * $b_1 + b_2 = b$	for example, $a^2 - b^2 = a^2 + ab - ab - b^2$
This allows us to then factor by grouping.	
$\log_b(a) = c \leftrightarrow b^c = a$ (whenever $a \neq 0$)	

These properties can be derived from the ones on the previous page and/or the definitions:

$$x^a x^b = x^{a+b}$$

$$\frac{x^a}{x^b} = x^{a-b}$$

$$\log_b(xy) = +\log_b(y) \quad (x, y \neq 0)$$

$$\log_b\left(\frac{x}{y}\right) = \log_b(x) - \log_b(y) \quad (x, y \neq 0)$$

$$(x^a)^b = x^{ab}$$

$$\log_b(x^y) = y \cdot \log_b(x) \quad (x \neq 0)$$

$$\log_b(x) = \frac{\log_c(x)}{\log_c(b)}$$

Rules for rewriting trigonometric expressions and for solving equations are not listed here at present.

Properties that apply to equations specifically:

$$a = b \leftrightarrow b = a$$

$$a = b \leftrightarrow a + c = b + c \quad a < b \leftrightarrow a + c < b + c$$

$$a = b \leftrightarrow a \cdot c = b \cdot c \quad (\text{whenever } c \neq 0) \quad a < b \leftrightarrow \begin{cases} a \cdot c < b \cdot c & \text{if } c > 0 \\ a \cdot c > b \cdot c & \text{if } c < 0 \end{cases}$$

$$a = b \leftrightarrow \frac{a}{c} = \frac{b}{c} \quad (\text{whenever } c \neq 0) \quad a < b \leftrightarrow \begin{cases} \frac{a}{c} < \frac{b}{c} & \text{if } c > 0 \\ \frac{a}{c} > \frac{b}{c} & \text{if } c < 0 \end{cases}$$

$$a = b \text{ and } c = d \leftrightarrow a + c = b + d \quad a = b \text{ and } c = d \leftrightarrow na + mc = nb + md \\ \text{for any numbers } n \text{ and } m$$

$$ab = 0 \leftrightarrow a = 0 \text{ or } b = 0$$